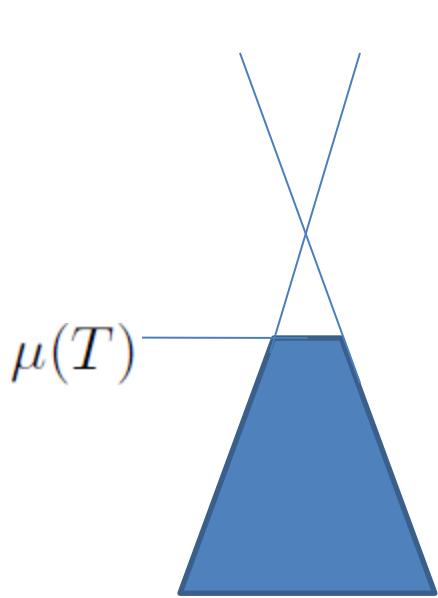


Thermodynamics of electron-hole liquids in graphene

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Coulomb renormalization



$$\varepsilon_s(p) = \mp vp \sim \frac{e^2}{r} \quad \text{if} \quad p \sim \frac{\hbar}{r}$$

Abrikosov, Beneslavsky 1971

Conzalez et al 1999

E. Mishchenko 2007

$$\varepsilon_s(p) = \mp vp[1 + g \ln(p_0/p)]$$

Lifshitz-Kosevich formula

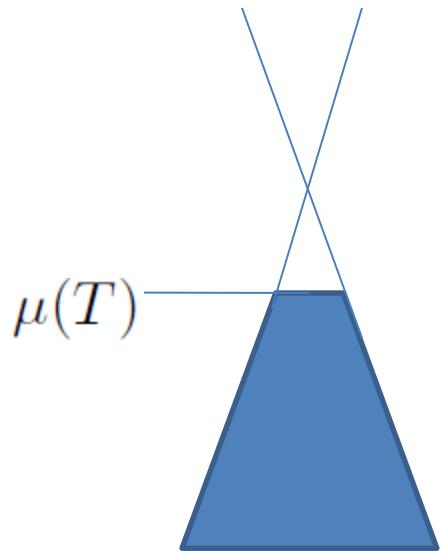
$$\tilde{M}(B) = \frac{2\pi n_0 S T}{B} \sum_{k \neq 0} \frac{\cos[kcA(\varepsilon_F)/e\hbar B]}{\sinh[2\pi^2 kc|m(\varepsilon_F)|T/e\hbar B]}$$

$$A(\varepsilon) = \pi \left(\frac{\varepsilon}{v} \right)^2 (1 - 2g \ln(p_0 v / \varepsilon))$$

$$m(\varepsilon) = \frac{1}{2\pi} \frac{dA(\varepsilon)}{d\varepsilon}$$

Coulomb renormalization

Yu, Katsnelson, Geim, Novoselov et al 2013



$$\varepsilon_s(p) = \mp vp[1 + g \ln(p_0/p)]$$

$$g = e^2 / 8\pi\hbar v \epsilon$$

$$p_0 \simeq 0.5 \times 10^8 \text{ cm}^{-1}$$

$$\epsilon \simeq 2.5 \div 8$$

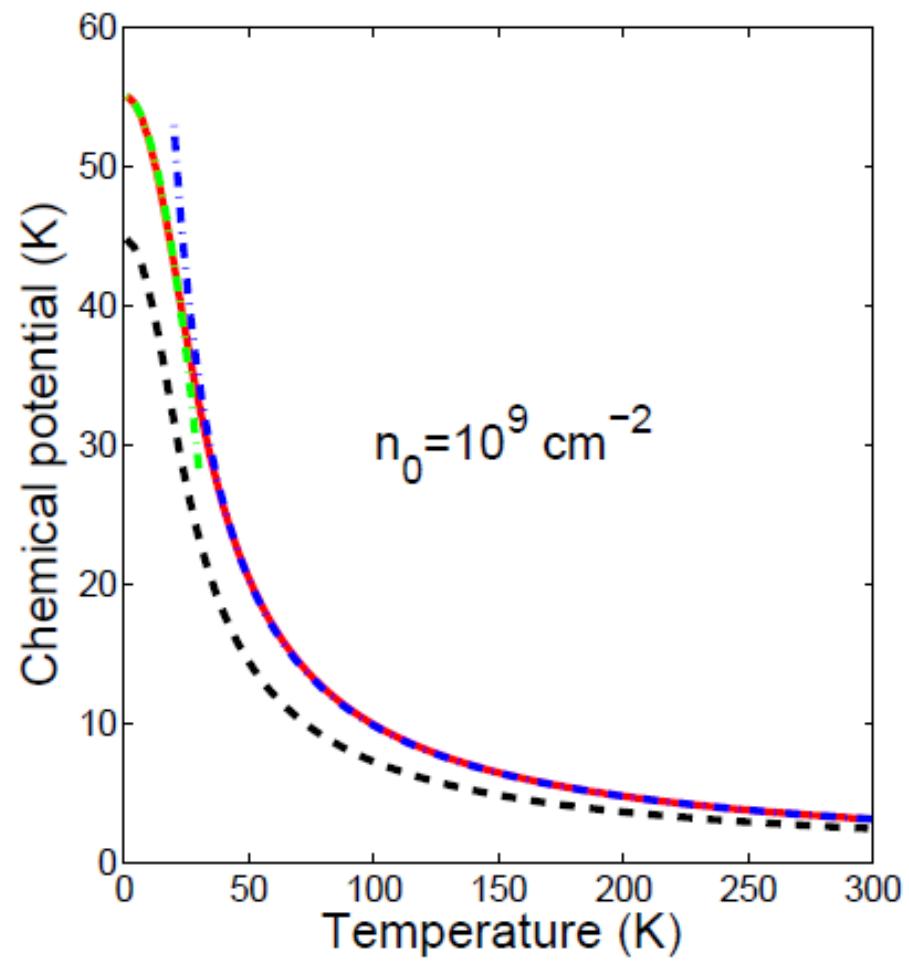
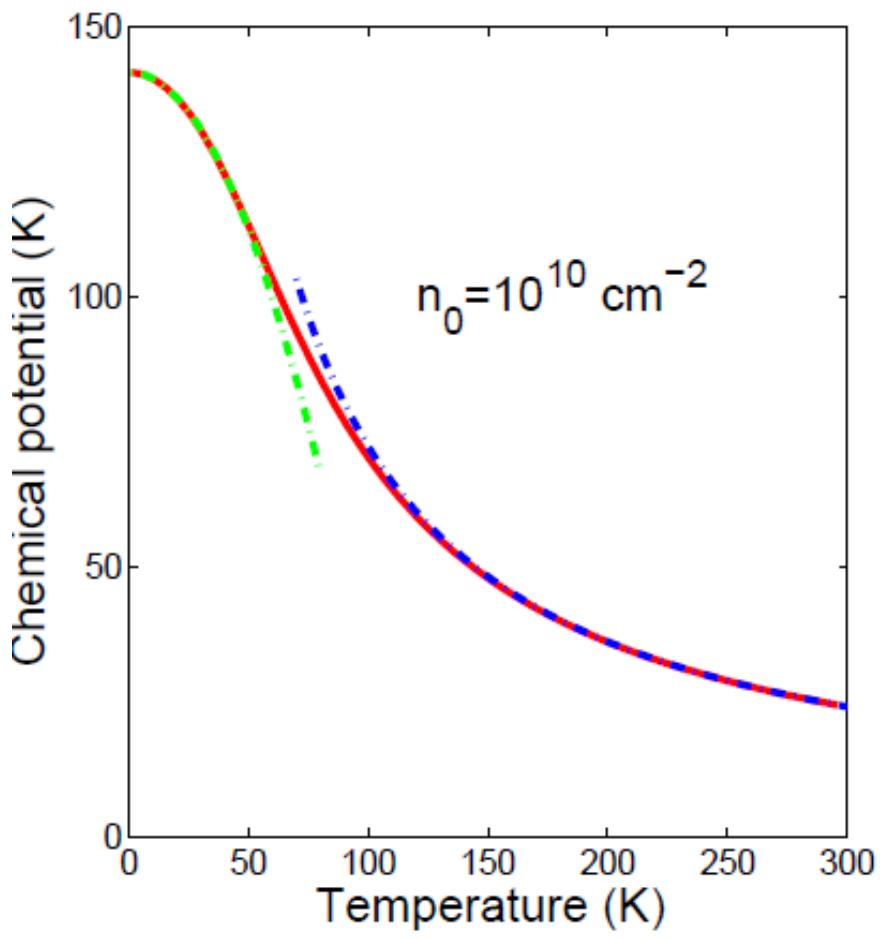
Chemical potential

$$\mu = \varepsilon_F - \frac{\pi^2}{6} \frac{T^2}{\varepsilon_F}$$

$$n_0 = \frac{p_F^2}{\pi \hbar^2} = \frac{1}{\pi} \left(\frac{\varepsilon_F}{\hbar v} \right)^2 [1 - 2g \ln(p_0 v / |\varepsilon_F|)]$$

$$|\mu| = \frac{\pi}{4 \ln 2} \frac{n_0 (\hbar v)^2}{T} [1 + 2g \ln(p_0 v / 2T)]$$

Chemical potential



Heat capacity

$$T \ll |\mu|$$

$$C_S^{(e)} = \frac{2\pi S |\varepsilon_F|}{3 (\hbar v)^2} T [1 - 2g \ln(p_0 v / |\varepsilon_F|)]$$

$$n_0 = \frac{p_F^2}{\pi \hbar^2} = \frac{1}{\pi} \left(\frac{\varepsilon_F}{\hbar v} \right)^2 [1 - 2g \ln(p_0 v / |\varepsilon_F|)]$$

$$T \gg |\mu|$$

$$E = \frac{\pi^2}{6 \ln 2} NT \quad \text{and} \quad C_S^{(e)} = \frac{\pi^2}{6 \ln 2} N$$